

magnitude too slow to produce  $v$ -weakening, except perhaps at temperatures of 500° to 700°C reached in experiments at coseismic slip velocities (4, 5, 14, 19).

The internal polycrystalline substructure of the nanospherules and nanofibers that we observed bears a striking similarity to microstructures found in shocked ductile metals (24). As in metals, the well-known ductility of calcite (25) may allow the ~5- to 20-nm substructure to form by progressive development of nano-cell walls from dense dislocation networks generated by crystal plasticity. Plastic deformation, fracturing, and abrasion presumably generated the observed nanospherules from the starting “gouge.” To explain the chaining of nanospherules, producing the observed fiber structure and CPO, we note that oriented attachment at coherent nanoparticle interfaces is widely reported as a mechanism by which nanocrystallites can rapidly coalesce to form single crystals (26, 27), also in calcite (28). On this basis, we suggest that the strong anisotropy in the surface energy of calcite produced similar preferred sintering (neck growth) at high-energy crystallographic interfaces between neighboring spherules (Fig. 3, B and C), leading to dynamic chaining and alignment of the lowest-energy (104) plane (29) parallel to the shear plane, and thus to the observed fibrous structure and CPO.

In principle, the mechanism of frictional slip that we propose (Fig. 3, A to C, and fig. S1) is similar to the Ashby-Verrall model for superplasticity by diffusion-accommodated grain boundary sliding (GBS) (Fig. 3D) (30), but allows for frictional GBS and for intergranular cavitation (porosity generation by dilatation) when diffusive mass transport is too slow to accommodate GBS. Our findings imply that nanocrystalline PSZs developed in calcite faults can produce  $v$ -weakening, and hence seismogenic fault friction, by a mechanism of cooperative nanogranular or nanofiber flow plus diffusive mass transfer (Fig. 3, A to C), even in the upper crust where temperatures are generally considered too low to support diffusion or superplasticity at active fault slip rates. The reason that these processes are observed in our experiments is because diffusive mass transfer is dramatically accelerated by the nanogranular nature of the slip-zone rock that forms, and by water-enhanced grain boundary diffusion. A similar mechanism can also be envisaged to operate at coseismic slip rates, where the high temperatures generated will promote solid-state diffusion. Given the abundant recent observations of nanogranular fault surfaces in tectonically active terrains (1–7), and the anomalously high rates of diffusion found in nanomaterials (15, 16), the proposed mechanism may be relevant not only to faults cutting calcite-rich rocks such as limestones, but to crustal seismogenesis in general.

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## SUPPLEMENTARY MATERIALS

[www.sciencemag.org/content/346/6215/1342/suppl/DC1](http://www.sciencemag.org/content/346/6215/1342/suppl/DC1)  
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## SOLID STATE THEORY

# Quantum spin Hall effect in two-dimensional transition metal dichalcogenides

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Quantum spin Hall (QSH) effect materials feature edge states that are topologically protected from backscattering. However, the small band gap in materials that have been identified as QSH insulators limits applications. We use first-principles calculations to predict a class of large-gap QSH insulators in two-dimensional transition metal dichalcogenides with 1T' structure, namely, 1T'-MX<sub>2</sub> with M = (tungsten or molybdenum) and X = (tellurium, selenium, or sulfur). A structural distortion causes an intrinsic band inversion between chalcogenide-p and metal-d bands. Additionally, spin-orbit coupling opens a gap that is tunable by vertical electric field and strain. We propose a topological field effect transistor made of van der Waals heterostructures of 1T'-MX<sub>2</sub> and two-dimensional dielectric layers that can be rapidly switched off by electric field through a topological phase transition instead of carrier depletion.

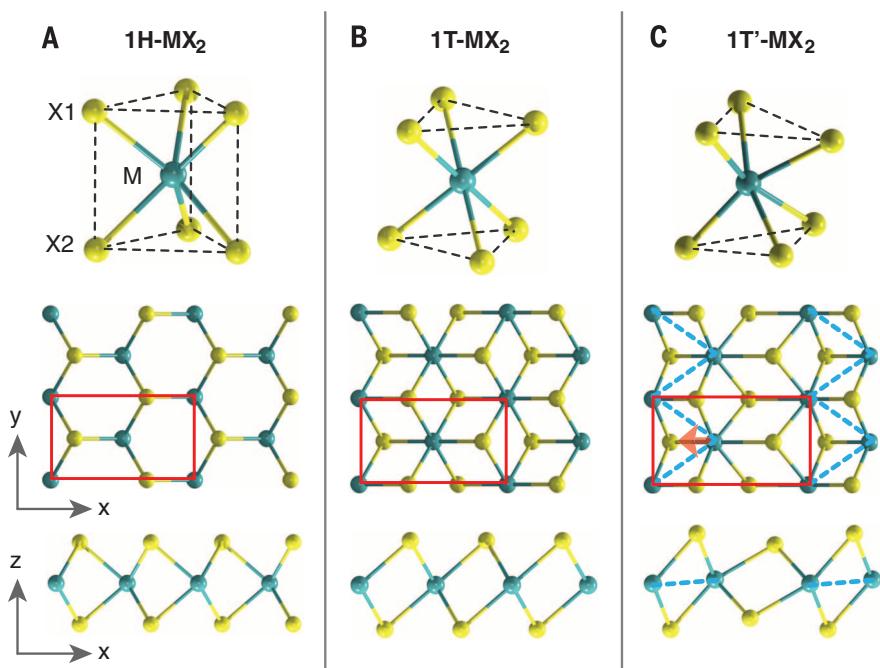
The discovery of graphene (1) has fuelled vigorous investigation of two-dimensional (2D) materials (2), revealing a wide range of extraordinary properties (3–5) and functionalities (6, 7). Owing to their atomic thickness, 2D materials can be horizontally patterned through chemical and mechanical techniques (8). Moreover, the weak van der Waals (vdW) interaction between adjacent layers enables vertical stacking of different 2D materials,

forming vdW heterostructures (9), which offer unprecedented opportunities for exploring quantum electronics at the nanoscale.

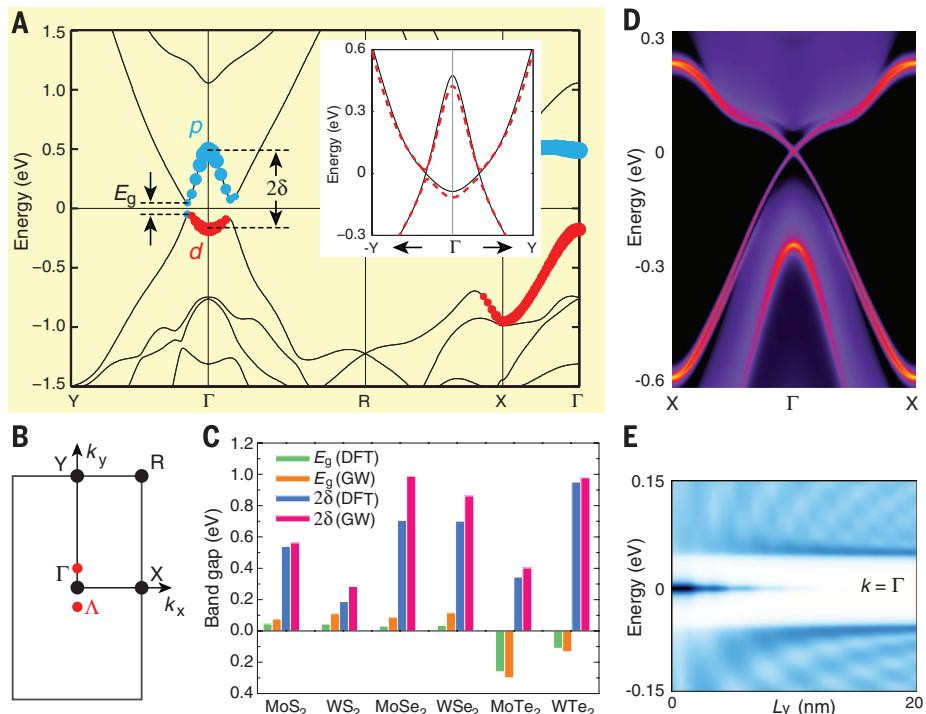
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**Fig. 1. Atomistic structures of monolayer transition metal dichalcogenides  $\text{MX}_2$ .** M stands for (W, Mo) and X stands for (Te, Se, S). (**A**) 1H- $\text{MX}_2$  in ABA stacking with  $P\bar{6}m2$  space group. (**B**) 1T- $\text{MX}_2$  in ABC stacking with  $P\bar{3}m1$  space group. (**C**) 1T'- $\text{MX}_2$ , distorted 1T- $\text{MX}_2$ , where the distorted M atoms form 1D zigzag chains indicated by the dashed blue line. The unit cell is indicated by red rectangles.



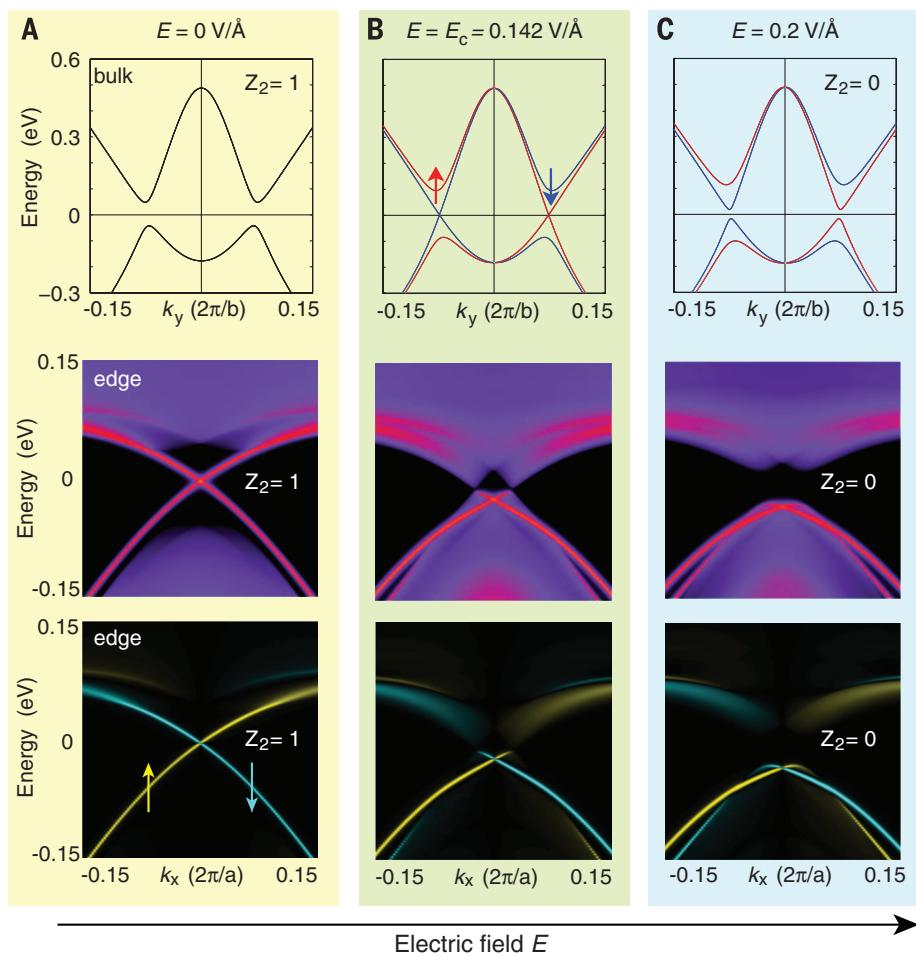
**Fig. 2. Calculated electronic structures of 1T'- $\text{MX}_2$ .** (**A**) Band structure and (**B**) Brillouin zone of 1T'- $\text{MoS}_2$ .  $E_g$ , fundamental gap;  $2\delta$ , inverted gap. The inset compares band structures with (red dashed line) and without (black solid line) spin-orbit coupling. Four time-reversal invariant momenta are marked by black dots and labeled as  $\Gamma$ , X, Y, and R. The locations of the fundamental gap are marked by red dots and labeled by  $\Lambda$ . (**C**) Fundamental gap ( $E_g$ ) and inverted gap ( $2\delta$ ) of all six 1T'- $\text{MX}_2$ . Detailed values are listed in table S1. (**D**) Edge density of states and (**E**) local density of states at  $\Gamma$  point as a function of distance away from the edge ( $L_y$ ). A sharp peak from edge states appears in the gap with a decay length of  $\sim 5$  nm.

Quantum spin Hall (QSH) insulators (10–16) have an insulating bulk but conducting edge states that are topologically protected from back-scattering by time-reversal symmetry. Quantized conductance through QSH edge states have been experimentally demonstrated in HgTe/CdTe (13, 14) and InAs/GaSb (17, 18) quantum wells. This could in principle provide an alternative route to quantum electronic devices with low dissipation. However, the realization of such QSH-based devices for practical applications is impeded by three critical factors: (i) band gaps of existing QSH insulators are too small, which limits the operating regime to low temperatures. This has motivated efforts to search for large-gap QSH insulators (19–26); (ii) the small number of conducting channels ( $e^2/h$  per edge, where  $e$  is the elementary charge and  $h$  is Planck's constant) results in a small signal-to-noise ratio; and (iii) efficient methods of fast on/off switching are lacking.

Here, we use first-principles calculations to show that 2D materials can provide a practical platform for developing topological electronic devices that may potentially overcome the above hurdles. Specifically, we predict a class of large-gap ( $\sim 0.1$  eV) QSH insulators in 2D transition metal dichalcogenides (TMDCs)  $\text{MX}_2$  with M = (W, Mo) and X = (Te, Se, S). We demonstrate the feasibility of a vdW-heterostructured topological field-effect transistor (vdW-TFET) made of 2D atomic layer materials. The proposed device exhibits a parametrically enhanced conductance through QSH edge channels in the “on” state and can be rapidly switched off via a topological phase transition by applying a vertical electric field. Our findings have potential applications in low-power quantum electronics and spintronics and may enable topological quantum computing based on Majorana fermions (27–30).

Monolayer TMDCs (31)– $\text{MX}_2$  with M = (W, Mo) and X = (Te, Se, S)—possess a variety of polytypic structures such as 1H, 1T, and 1T' (32, 33) shown in Fig. 1. The most-studied 1H structure is a sandwich of three planes of 2D hexagonally packed atoms, X-M-X, forming Bernal (ABA) stacking. In contrast, the three atomic planes in the 1T structure form rhombohedral (ABC) stacking. It has been known that the 1T structure in  $\text{MX}_2$  is typically unstable in free-standing condition and undergoes a spontaneous lattice distortion in the  $x$  direction to form a period-doubling  $2 \times 1$  distorted structure—i.e., the 1T' structure, consisting of 1D zigzag chains along the  $y$  direction (Fig. 1C) (33); this structure is the subject of our work.

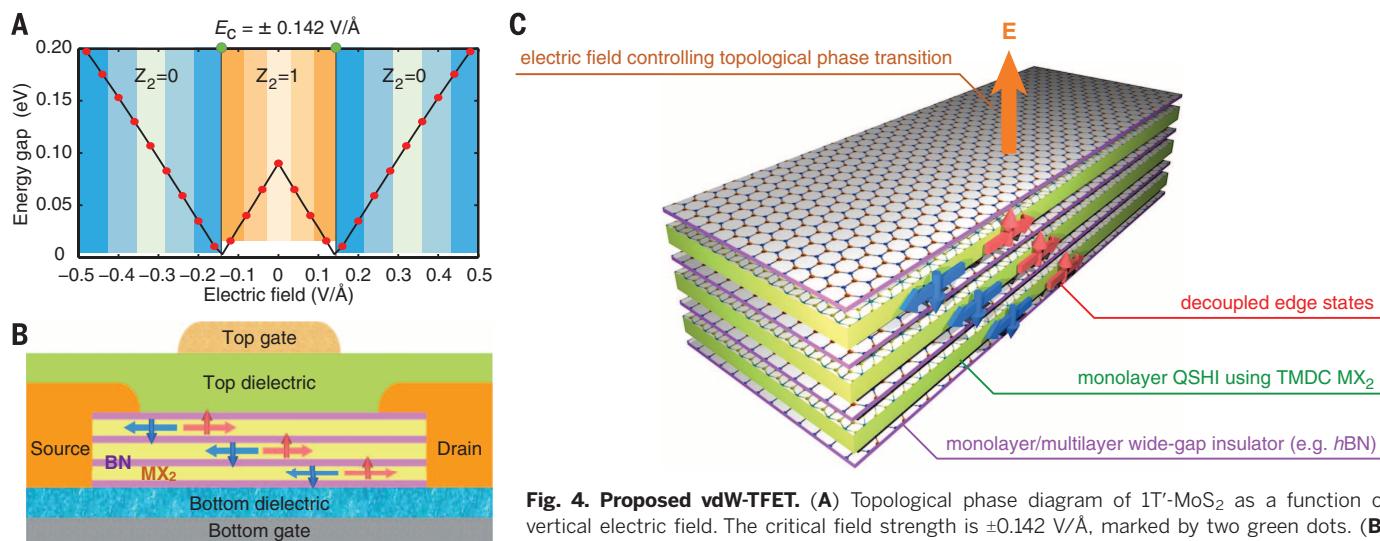
The electronic structures of various 1T'- $\text{MX}_2$  materials were obtained by many-body perturbation theory calculations (34). Figure 2A shows a typical band structure of 1T'- $\text{MX}_2$  using 1T'- $\text{MoS}_2$  as an example, and the results of the other five compounds are shown in fig. S1. Unlike its 1H or 1T counterparts, 1T'- $\text{MoS}_2$  is a semiconductor with a fundamental gap ( $E_g$ ) of about 0.08 eV, located at  $\Lambda = \pm(0, 0.146)\text{\AA}^{-1}$



**Fig. 3. Vertical electric field induced a topological phase transition.** Shown are calculations for monolayer 1T'-MoS<sub>2</sub> under electric fields of (A) 0, (B) 0.142, and (C) 0.2 V/Å, respectively. The first, second, and third rows show the bulk band structure, edge density of states, and edge spin polarization, respectively.

(red dots in Fig. 2B). The conduction and valence bands display a camelback shape near  $\Gamma$  in the 2D Brillouin zone (BZ) (see Fig. 2B), suggestive of band inversion with a large inverted gap ( $\Delta$ ) at  $\Gamma$  of about 0.6 eV. The fundamental gap ( $E_g$ ) and inverted gap ( $\Delta$ ) of all six 1T'-MX<sub>2</sub> are shown in Fig. 2C and listed in table S1. The inverted gap ( $\Delta$ ) was later used in the fitting of a low-energy  $k \cdot p$  model (34). Because the 1T' structure has inversion symmetry, we calculated the  $Z_2$  index (0 or 1, indicating trivial or non-trivial topology, respectively) based on the parity criterion (35) of valence bands (fig. S2) and found  $Z_2 = 1$ , indicating that 2D 1T'-MX<sub>2</sub> materials are in the QSH insulator phase.

To understand the origin of the inverted band structure near  $\Gamma$ , we analyzed the orbital character of the bands and found that the valence band mainly consists of metal  $d$ -orbitals and the conduction band mainly consists of chalcogenide  $p$  orbitals, as expected. The unexpected band inversion arises from the period doubling of the metal chain in the 1T' structure, which lowers the metal  $d$  orbital below chalcogenide  $p$  orbital (Fig. 2A) around  $\Gamma$ . The large band inversion at  $\Gamma$  (~0.6 eV) is an intrinsic characteristic of the 1T' structure and already takes place without including spin-orbit interaction in the first-principles calculations. In the absence of spin-orbit coupling, this band inversion leads to the appearance of two Dirac cones centered at finite momenta on Y- $\Gamma$ -Y in 2D BZ. Spin-orbit coupling then opens up a fundamental gap of 0.08 eV at the Dirac points (Fig. 2A, inset, and fig. S3), leading to a QSH insulator through a similar mechanism as the Kane-Mele model for graphene (10); we show that this is the case by using a low-energy  $k \cdot p$  Hamiltonian (34) (fig. S4). In addition to MoS<sub>2</sub>, we found that all other five 1T'-MX<sub>2</sub> have  $Z_2$  nontrivial band topology.



**Fig. 4. Proposed vdW-TFET.** (A) Topological phase diagram of 1T'-MoS<sub>2</sub> as a function of vertical electric field. The critical field strength is  $\pm 0.142$  V/Å, marked by two green dots. (B) Schematic of vdW-TFET. The central component (C) is a vdW heterostructure of alternating MX<sub>2</sub> layers, with horizontal width as narrow as ~20 nm. Carriers (charge or spin) are injected from the source electrode and ejected into the drain electrode. On/off switch is controlled by vertical electric field through the top and bottom gates. Mono-/multilayer wide-gap insulators effectively screen the interaction between adjacent MX<sub>2</sub> layers, preventing them from detrimentally topological phase change and parametrically increasing the number of edge channels.

The QSH insulator phase in 2D 1T'-MX<sub>2</sub> leads to helical edge states that are protected from localization and elastic backscattering by time-reversal symmetry. Figure 2D displays the edge states of 1T'-MoS<sub>2</sub> obtained from surface Green's function calculations (34), showing a pair of counter-propagating edge modes with a high velocity of  $\sim 1.0 \times 10^5$  m/s that cross at  $\Gamma$  and carry opposite spin polarizations. From the local density of states in Fig. 2E, we find the decay length of these helical edge states to be as short as 5 nm. The short localization length can greatly reduce scattering with bulk states (36), hence increasing the transport lifetime. Similar results were found for five other TMDCs (figs. S5 and S6).

The inverted bands between chalcogenide's *p* and metal's *d* orbitals located on well-separated planes offer a facile mechanism to control topological electronic properties by electric field, which is highly desirable for vdW devices. Based on first-principles calculations, we found that a vertical electric field indeed induces a topological phase transition in 1T'-MX<sub>2</sub>, as shown in Fig. 3 for 1T'-MoS<sub>2</sub>. Here, the electric field breaks inversion symmetry and introduces a strong Rashba splitting of the doubly degenerate bands near the fundamental gap  $E_g$  at the  $\Lambda$  points. As the field increases,  $E_g$  first decreases to zero at a critical field strength of 0.142 V/Å and then reopens (see Fig. 4A). This gap-closing transition induces a topology change to a trivial phase (11, 37), leading to the destruction of helical edge states.

The above findings point to the possibility of an all-electrical control of the on/off charge/spin conductance of helical edge states, which would have substantial implications for QSH-based devices (38–43). Here, we propose a TFET based on vdW heterostructures of 2D TMDCs and 2D wide-gap insulators. The proposed device is sketched in Fig. 4B, where the top and bottom gates supply the vertical electric field to control the on/off function. Two-dimensional wide-gap insulators such as hexagonal boron nitride (hBN) (44) electrically insulate adjacent QSH layers, hence protecting parallel helical edge channels from being gapped by interlayer hybridization. This can parametrically increase the number of edge transport channels. Under ideal conditions, this device will support dissipationless charge/spin transport in the “on” state ( $Z_2 = 1$ ), with a quantized conductance of  $2Ne^2/h$ , where  $N$  is the number of QSH layers. Applying a moderate electric field will transform 1T'-MX<sub>2</sub> into an ordinary insulator ( $Z_2 = 0$ ) and turn the edge conduction off (Fig. 4A).

The proposed vdW-TFET may possess important technical advantages, thanks to an operation mechanism that is fundamentally different from traditional metal-oxide-semiconductor FETs (MOS-FET). MOS-FET works by injecting/depleting free carrier beneath the gate, with a resistor-capacitor-type response time influenced by carrier concentration and mobility in the working channel, whereas our vdW-TFET works by switching

the presence/absence of topologically protected conduction channels. The electric field-induced topological phase transition can happen very rapidly, with an electronic response time scale (45, 46). In addition, the vdW heterostructure and the 2D nature of vdW-TFET make it convenient to both vertically and horizontally pattern devices at a large scale. The short decay length of helical edge states allows the minimum horizontal feature size of vdW-TFET to be  $\sim 20$  nm, enabling high device density on a chip. Horizontally patterned TFET devices of such nanoscale size have large edge-to-area ratios, which will greatly reduce the contribution of thermally populated bulk carriers to the total electric current and hence enhance the on/off ratio. The predicted QSH insulators and their vdW heterostructures may provide a platform for realizing low-dissipation quantum electronics and spintronics (38–43).

From a materials perspective, the 1T' structure in monolayer MoS<sub>2</sub> has recently been observed in high-resolution transmission electron microscopy experiments (33). We have checked the structural stability of 1T' by carrying out first-principles calculations (fig. S7). Although MoS<sub>2</sub>, MoSe<sub>2</sub>, MoTe<sub>2</sub>, WS<sub>2</sub>, and WSe<sub>2</sub> are more stable in the 1H structure, we find that there exists a large energy barrier of more than 1 eV/MX<sub>2</sub> between 1T' and 1H for all MX<sub>2</sub>, suggesting that the 1T' structure can be stabilized under appropriate chemical (47), thermal, or mechanical conditions. Moreover, we found that the 1T structure is unstable and will spontaneously relax to 1T', like in a Peierls distortion. We also verified the stability of the 1T' structure by computing its phonon dispersion (fig. S8). The absence of imaginary frequencies throughout the 2D BZ provides direct evidence of the structural stability in all 1T'-MX<sub>2</sub>.

Encouragingly, the desired 1T' structure with intrinsic band inversion is the natural ground-state structure of WTe<sub>2</sub> (37), also confirmed by our stability calculation. Although monolayer WTe<sub>2</sub> was found to be a semimetal from our calculation, the small negative fundamental gap can be easily lifted by a tensile strain as small as  $\sim 1\%$  (fig. S9). We also found that hBN used as a dielectric in the aforementioned vdW-TFET device has little effect on the electronic structure of 1T'-WTe<sub>2</sub> near the Fermi level (fig. S10). These attractive features make WTe<sub>2</sub> potentially the most promising 2D TMDC for realizing the QSH effect and related vdW devices.

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## SUPPLEMENTARY MATERIALS

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## Supplementary Materials for

### **Quantum spin Hall effect in two-dimensional transition metal dichalcogenides**

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## Methods

### S1. Ground-state atomic structures of monolayer transition metal dichalcogenides $1T'$ -MX<sub>2</sub>

Ground-state atomic structures of all six monolayer transition metal dichalcogenides  $1T'$ -MX<sub>2</sub> were fully relaxed using first-principles density functional theory (DFT) (48, 49). The calculations were performed by the Vienna Ab initio Simulation Package (VASP) (50, 51) with projector-augmented wave method (52) and exchange-correlation functional in the Perdew-Berke-Ernzerhof's form (53) within the generalized-gradient approximation (54, 55). We used an energy cutoff of 400 eV and maximum residual force less than 0.001 eV/Å. The Monkhorst-Pack  $k$ -point sampling (56) of  $8 \times 8 \times 1$  was adopted for the Brillouin zone integration, and a large vacuum region of more than 16 Å was applied to the plane normal direction in order to minimize image interactions from the periodic boundary condition. Moreover, phonon dispersion curves were calculated by first-principles density-functional perturbation theory and the results are shown in Fig. S8 for all six materials.

### S2. Bulk electronic structure of monolayer transition metal dichalcogenides $1T'$ -MX<sub>2</sub>

We first computed the electronic band structures of monolayer transition metal dichalcogenides  $1T'$ -MX<sub>2</sub> using first-principles DFT. Since the calculated DFT band structures only provide qualitative electronic structure for quasi-particles such as electrons and holes, we further computed quasi-particle band structures using more accurate method, namely, many-body perturbation theory within Hedin's G<sub>0</sub>W<sub>0</sub> approximation (57, 58). The results are shown in Fig. 2A for monolayer  $1T'$ -MoS<sub>2</sub> and Fig. S1 for all six materials. Fundamental gap ( $E_g$ ) and inverted gap ( $\Delta$ ) of monolayer transition metal dichalcogenides  $1T'$ -MX<sub>2</sub> are collected in Table S1 and Fig. 2C.

### S3. Electronic structure of edge states in monolayer transition metal dichalcogenides $1T'$ -MX<sub>2</sub>

The Z<sub>2</sub> trivial/nontrivial band topology has distinct consequence on the helical edge state. To reveal the helical edge states of monolayer  $1T'$ -MX<sub>2</sub> explicitly, we performed iterative Green's function calculations (59) using tight-binding Hamiltonian (60, 61) constructed from many-body perturbation theory with the GW approximation (57, 58), where we extracted the edge density of states, spin polarization, and decay length of the helical edge states. The results are shown in Fig. 3 for monolayer  $1T'$ -MoS<sub>2</sub> and Fig. S5 and Fig. S6 for all six materials. Furthermore, to investigate the effect of vertical electric field on the electronic structure of monolayer  $1T'$ -MoS<sub>2</sub> QSHI, we introduce a corresponding change in the diagonal elements of first-principles tight-binding Hamiltonian. This approach is validated by comparing with direct self-consistent first-principles calculations under the same electric field. In addition, we found the electric field has negligible impact on ionic positions.

### S4. Z<sub>2</sub> invariant of monolayer transition metal dichalcogenides $1T'$ -MX<sub>2</sub>

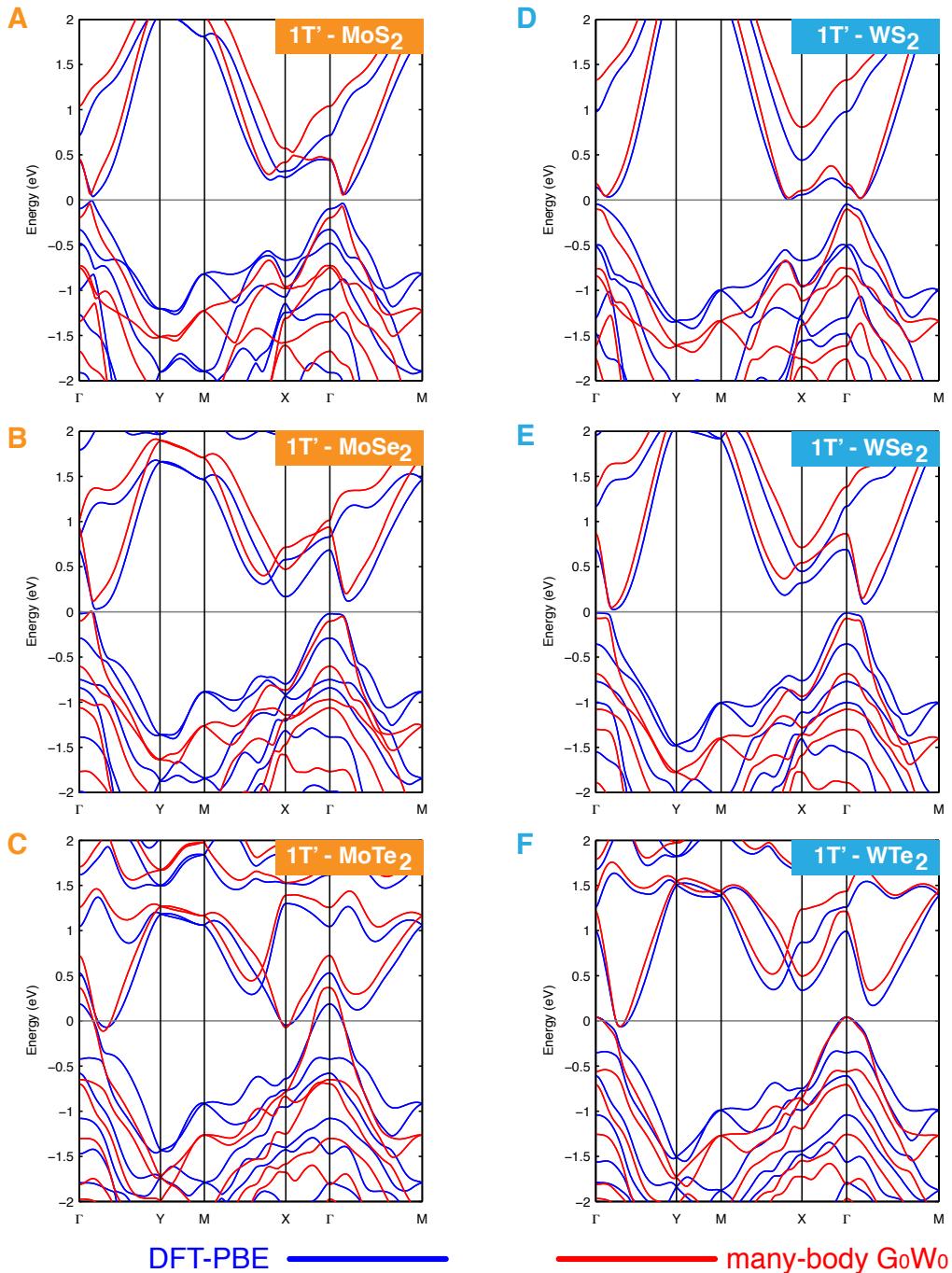
The Z<sub>2</sub> invariant was obtained by explicitly calculating band parity of the materials with inversion symmetry (35). The results are shown in Fig. S2 for all six materials with inversion center located at the middle of the bond formed by two transition metal atoms in the quasi-one dimensional chain along y direction. We also cross-checked all the results by the  $n$ -field method (62).

### S5. $k \cdot p$ model for monolayer transition metal dichalcogenides $1T'$ -MX<sub>2</sub>

The valence band mainly consists of  $d$ -orbitals of M atoms, while the conduction band mainly consists of  $p_y$ -orbitals of X atoms. The origin of such inversion roots in the formation of quasi-one dimensional transition metal chains in the 1T' structure, which lowers M's  $d$  orbital below p X's  $p$  to with respect to the original 1T structure, leading to the band inversion at  $\Gamma$  point (Fig. S3). By analyzing the symmetry properties of these bands, we develop a low-energy  $k \cdot p$  Hamiltonian for 1T'-MX<sub>2</sub>,

$$H = \begin{pmatrix} E_p(k_x, k_y) & 0 & -iv_1\hbar k_x & v_2\hbar k_y \\ 0 & E_p(k_x, k_y) & v_2\hbar k_y & -iv_1\hbar k_x \\ iv_1\hbar k_x & v_2\hbar k_y & E_d(k_x, k_y) & 0 \\ v_2\hbar k_y & iv_1\hbar k_x & 0 & E_d(k_x, k_y) \end{pmatrix},$$

where  $E_p = -\delta - \frac{\hbar^2 k_x^2}{2m_x^p} - \frac{\hbar^2 k_y^2}{2m_y^p}$ , and  $E_d = \delta + \frac{\hbar^2 k_x^2}{2m_x^d} + \frac{\hbar^2 k_y^2}{2m_y^d}$ . Here  $\delta < 0$  corresponds to the  $d$ - $p$  band inversion. By fitting with first-principles band structure in Fig. 2A, we obtain the parameters:  $\delta = -0.33$  eV,  $v_1 = 3.87 \times 10^5$  m/s,  $v_2 = 0.46 \times 10^5$  m/s,  $m_x^p = 0.50 m_e$ ,  $m_y^p = 0.16 m_e$ ,  $m_x^d = 2.48 m_e$ , and  $m_y^d = 0.37 m_e$ , where  $m_e$  is the free electron mass. Fig. S4 shows the comparison of band structures obtained from first-principles GW calculations and the  $k \cdot p$  model.



**Fig. S1.**

Electronic band structure of monolayer transition metal dichalcogenides 1T'- $\text{MX}_2$ . Blue lines stand for first-principles density-functional theory calculations. Red lines stand for many-body  $\text{G}_0\text{W}_0$  theory calculations.

A		
$\Gamma_i$	parity $\xi_{2m}$ of occupied bands	$\delta_i = \prod_m \xi_{2m}$
$\Gamma$	$+ - - + - + + - - + + + - - + + - +$	$+$
X	$- + + - + - + + - + - + + + - - -$	$-$
Y	$+ - + - + - + - + - + + - + + -$	$-$
R	$+ - + - + - + - + - + - + + - + -$	$-$
$Z_2$ invariant v: $(-1)^v = \prod_i \delta_i$		$v = 1$

$\Gamma_i$	parity $\xi_{2m}$ of occupied bands	$\delta_i = \prod_m \xi_{2m}$
$\Gamma$	$+ - + - + + - + - + + - + + - +$	$+$
X	$- + + - + + + - + + - + - + + -$	$-$
Y	$+ - + - + - + + - + + - + - + +$	$-$
R	$- + + - + - + + - + - + + - + +$	$-$
$Z_2$ invariant v: $(-1)^v = \prod_i \delta_i$		$v = 1$

$\Gamma_i$	parity $\xi_{2m}$ of occupied bands	$\delta_i = \prod_m \xi_{2m}$
$\Gamma$	$+ - + - + + - + - + + - + + - +$	$+$
X	$- + + - + - + + - + - + + - + -$	$-$
Y	$+ - + - + - + + - + + - + - + -$	$-$
R	$- + + - + - + + - + - + + - + -$	$-$
$Z_2$ invariant v: $(-1)^v = \prod_i \delta_i$		$v = 1$

$\Gamma_i$	parity $\xi_{2m}$ of occupied bands	$\delta_i = \prod_m \xi_{2m}$
$\Gamma$	$+ - - + - + + - - + + + - - + +$	$+$
X	$- + + - - + - + - + - + + + - + -$	$-$
Y	$- + + - - + + + - + - + + + - + -$	$-$
R	$- + + + - + + - + - + + + - + -$	$-$
$Z_2$ invariant v: $(-1)^v = \prod_i \delta_i$		$v = 1$

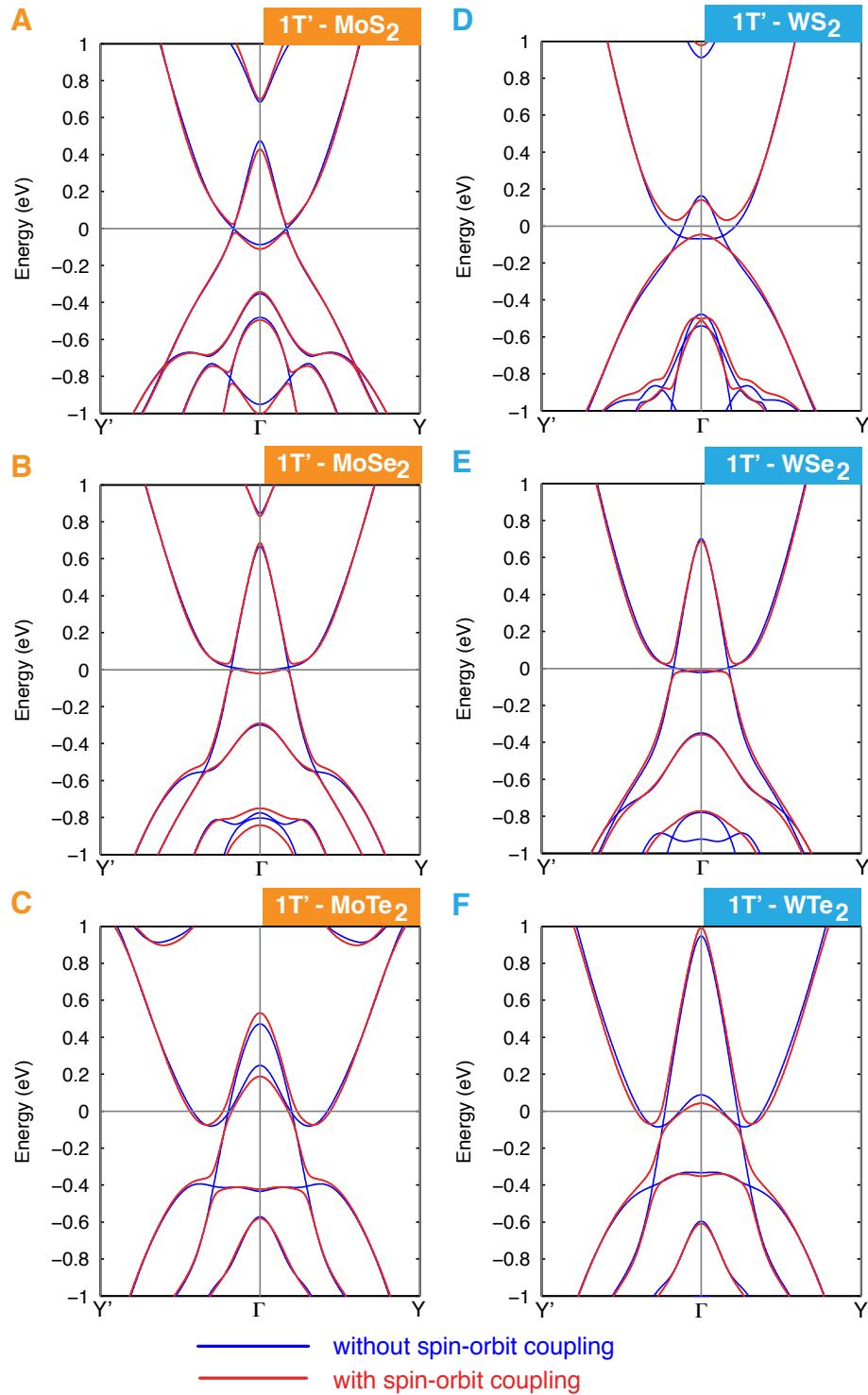
$\Gamma_i$	parity $\xi_{2m}$ of occupied bands	$\delta_i = \prod_m \xi_{2m}$
$\Gamma$	$+ - + - - + + - + - + + - + + - +$	$+$
X	$- + + - - + - + - + + + - + - + +$	$-$
Y	$- + + - - + + + - + + - - + + - -$	$-$
R	$- + - + + - + + - + - + + - + -$	$-$
$Z_2$ invariant v: $(-1)^v = \prod_i \delta_i$		$v = 1$

$\Gamma_i$	parity $\xi_{2m}$ of occupied bands	$\delta_i = \prod_m \xi_{2m}$
$\Gamma$	$+ - + - - + + - + - + + - + + - +$	$+$
X	$- + - + + - + - + - + - + - + + -$	$-$
Y	$- + + - - + + + - + + - - + - + -$	$-$
R	$- + + + - - + + - + + - - + - + -$	$-$
$Z_2$ invariant v: $(-1)^v = \prod_i \delta_i$		$v = 1$

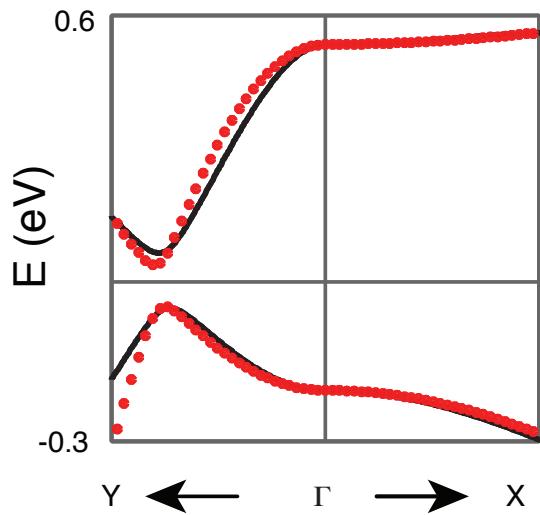
Fig. S2.

Parity tables for monolayer transition metal dichalcogenides 1T'-MX<sub>2</sub> at time-reversal invariant momenta, and the corresponding Z<sub>2</sub> invariants, v. All Z<sub>2</sub> invariants are 1, indicating all six 1T'-MX<sub>2</sub> are topologically nontrivial. We choose the inversion center at the middle of the short M-M bond formed by two transition metal atoms.



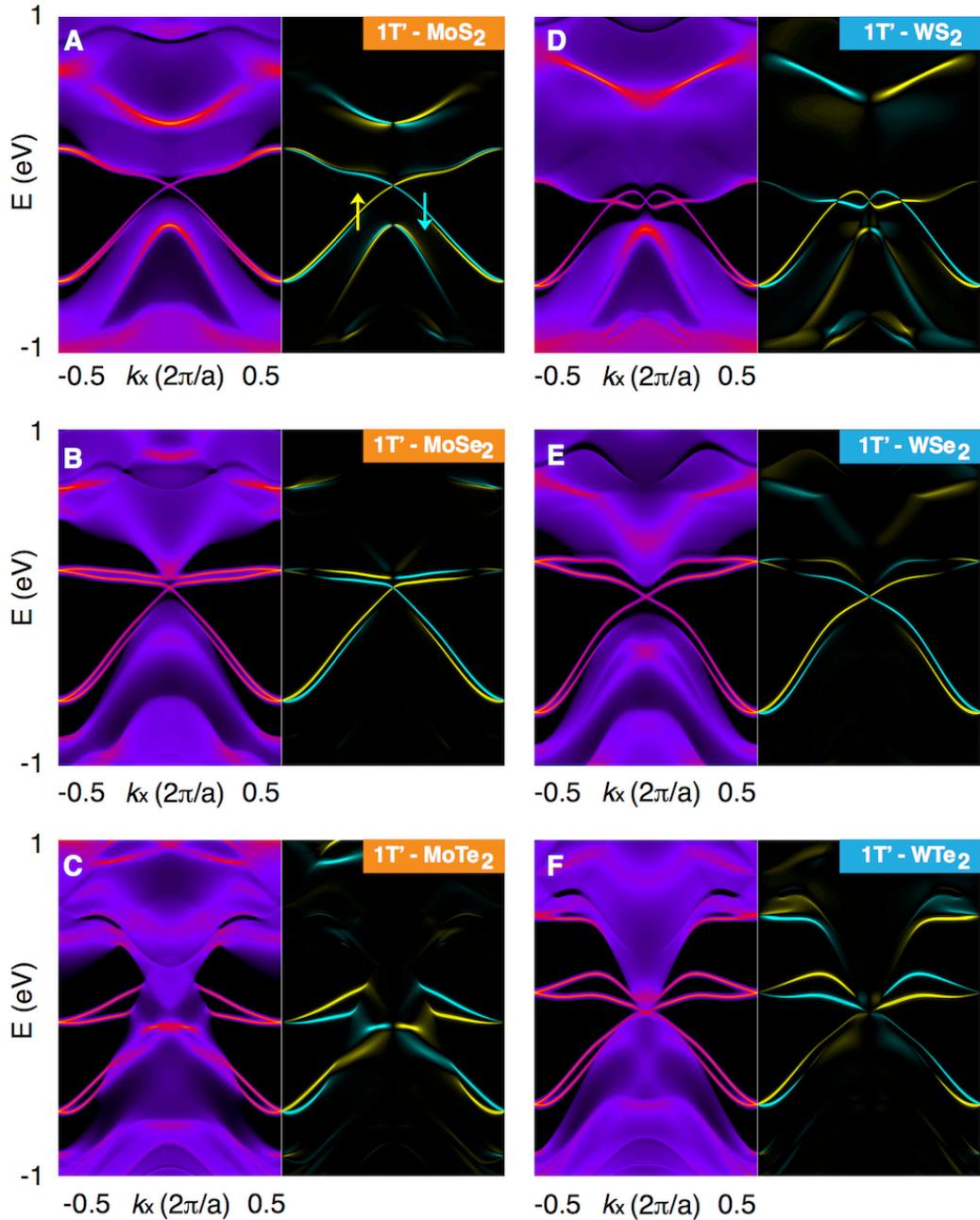
**Fig. S3.**

Electronic band structure of monolayer transition metal dichalcogenides 1T'-MX<sub>2</sub> with and without spin-orbit coupling. The calculations were performed by first-principles density-functional theory with the PBE exchange-correlation functional.



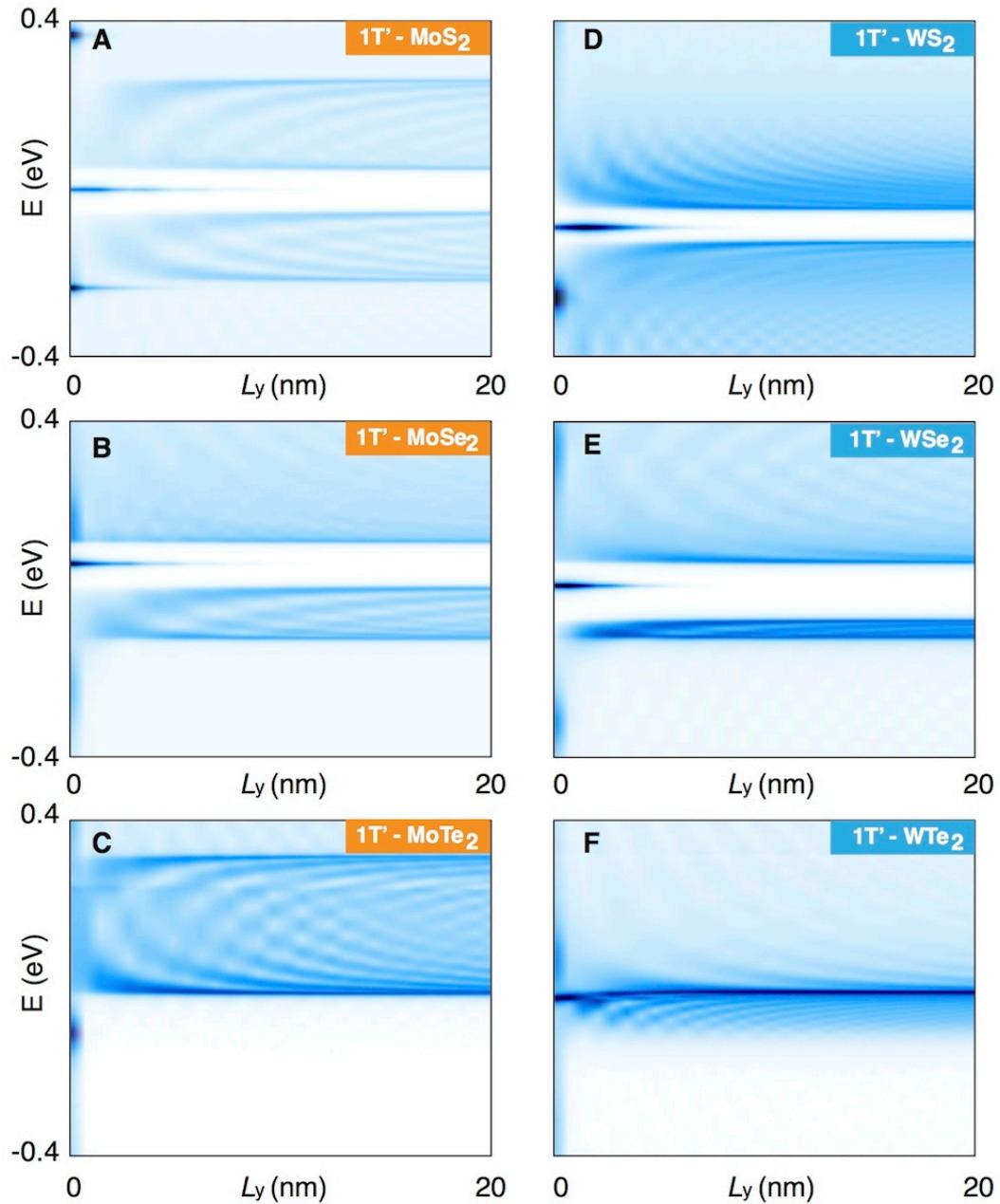
**Fig. S4.**

Comparison of band structures obtained from first-principles GW calculation (black line) and the fitted  $k \cdot p$  Hamiltonian (red dots) for 1T'-MoS<sub>2</sub>.



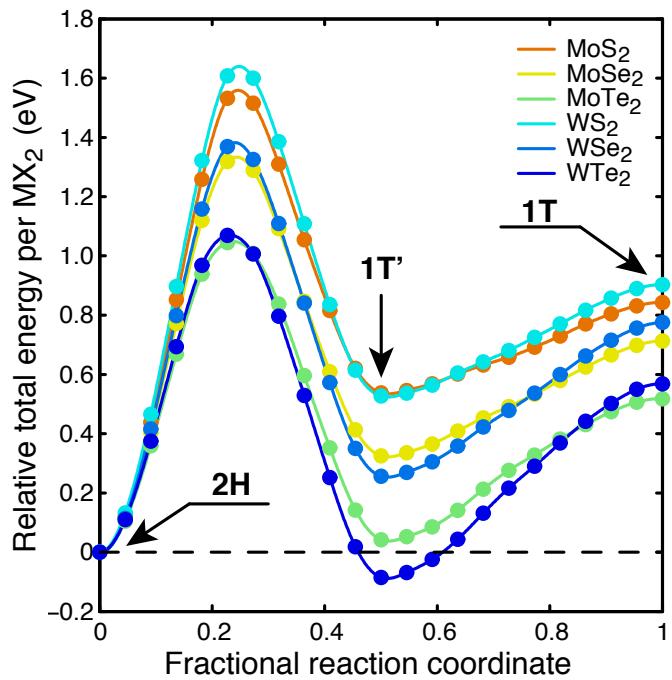
**Fig. S5.**

Electronic structure of helical edge states in monolayer transition metal dichalcogenides 1T'-MX<sub>2</sub>. For each MX<sub>2</sub>, the left subpanel shows the density of states while the right subpanel shows the corresponding spin polarization. These helical edge states are a manifestation of nontrivial topology of monolayer 1T'-MX<sub>2</sub>.



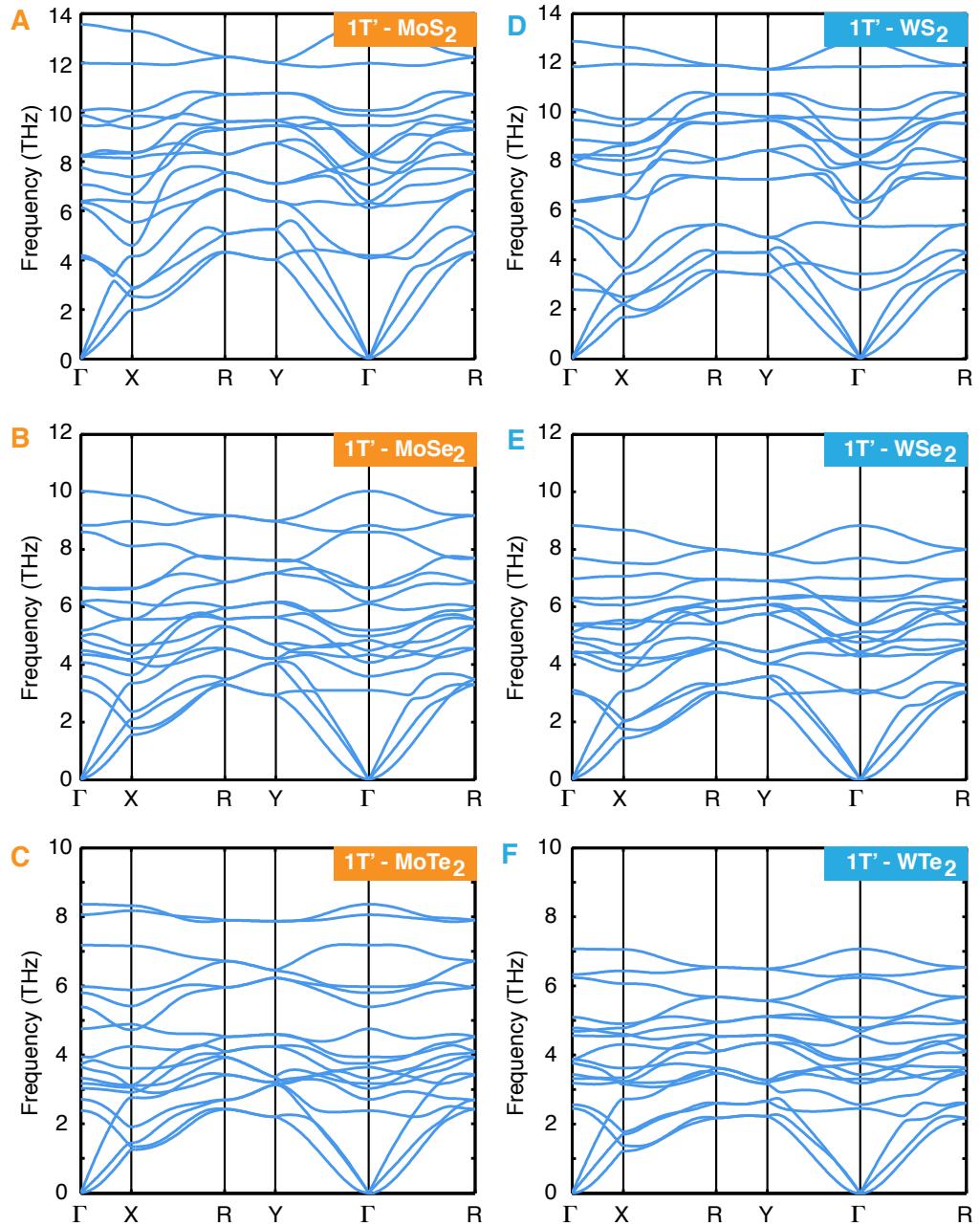
**Fig. S6.**

Local density of states as function of penetration depth away from the edge at  $L_y=0$  in monolayer transition metal dichalcogenide 1T'-MX<sub>2</sub>. Due to the semi-metallic nature of 1T'-MoTe<sub>2</sub> and 1T'-WTe<sub>2</sub>, local density of states from edge and bulk are entangled with each other. Therefore, the decay lengths of their edge states are not accessible.



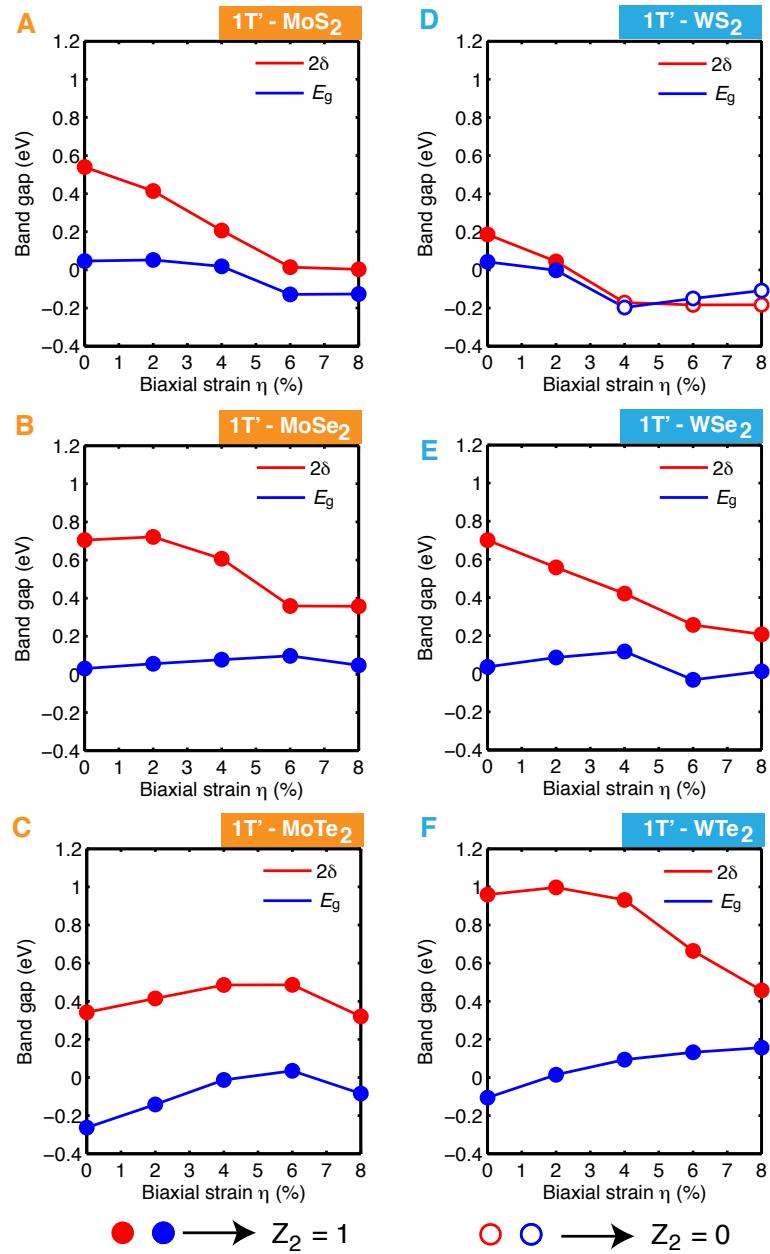
**Fig. S7.**

Structural stability of monolayer transition metal dichalcogenide 1T'-MX<sub>2</sub>: relative total energy per MX<sub>2</sub> as a function of fractional reaction coordinate.



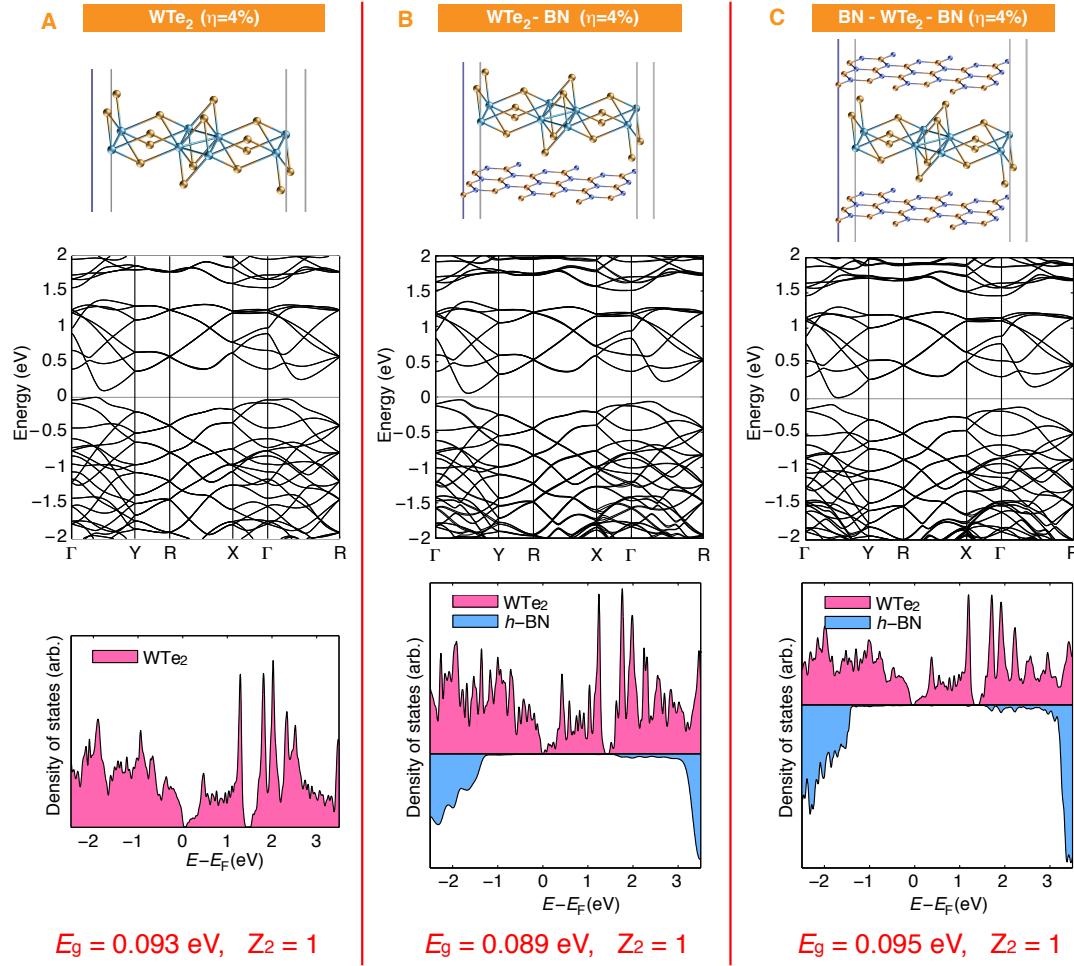
**Fig. S8.**

Phonon dispersion curves of monolayer transition metal dichalcogenide 1T'-MX<sub>2</sub>. The absence of imaginary frequency demonstrates the structural stability of all six monolayer 1T'-MX<sub>2</sub>.



**Fig. S9.**

Effect of biaxial strain on fundamental gap ( $E_g$ ), inverted gap ( $2\delta$ ), and  $Z_2$  invariant of  $1T'$ -MX<sub>2</sub>. Positive inverted gap ( $2\delta$ ) indicates  $Z_2=1$  and positive  $E_g$  indicates insulator.



**Fig. S10.**

Effect of van der Waals heterostacking with hexagonal BN monolayers on electronic structure, projected density of states, fundamental band gap ( $E_g$ ), and  $Z_2$  invariant of 1T'-WTe<sub>2</sub> under 4% biaxial strain. The supercell was constructed by 2x2 1T'-WTe<sub>2</sub> and  $3\sqrt{3}\times 3$  BN monolayers under 4% biaxial strain to minimize the lattice mismatch for first-principles calculations. **(A)** biaxially-strained monolayer 1T'-WTe<sub>2</sub>. **(B)** strained 1T'-WTe<sub>2</sub> stacked on hexagonal BN monolayer. **(C)** strained 1T'-WTe<sub>2</sub> sandwiched by two hexagonal BN layers. It clearly shows that BN monolayers have negligible effect on the electronic structure of 1T'-WTe<sub>2</sub> in a wide energy range around the Fermi level, demonstrating hexagonal BN sheets as ideal dielectric layers for the experimental realization of van der Waals heterostructure-based topological field effect transistor.

1T' phase	Fundamental gap ( $E_g$ , eV)		Inverted gap ( $2\delta$ , eV)	
	DFT-PBE	$G_0W_0$	DFT-PBE	$G_0W_0$
WTe <sub>2</sub>	-0.112	-0.133	0.952	0.978
MoTe <sub>2</sub>	-0.262	-0.300	0.344	0.403
WSe <sub>2</sub>	0.036	0.116	0.701	0.863
MoSe <sub>2</sub>	0.031	0.088	0.706	0.988
WS <sub>2</sub>	0.044	0.110	0.187	0.284
MoS <sub>2</sub>	0.045	0.076	0.540	0.562

**Table S1.**

Fundamental gap ( $E_g$ ) and inverted gap ( $2\delta$ ) of monolayer transition metal dichalcogenides 1T'-MX<sub>2</sub> calculated by first-principles density-functional theory with PBE exchange-correlation functional and many-body perturbation theory within the  $G_0W_0$  approximation.

WTe2	MoTe2
1.0	1.0
6.314769 0.000000 0.000000	6.382718 0.000000 0.000000
0.000000 3.492485 0.000000	0.000000 3.450605 0.000000
0.000000 0.000000 20.160000	0.000000 0.000000 20.160000
W Te	Mo Te
2 4	2 4
Selective dynamics	Selective dynamics
Direct	Direct
0.821873 0.750000 0.495163 T T T	0.818044 0.750000 0.495460 T T T
0.178127 0.250000 0.504838 T T T	0.181956 0.250000 0.504540 T T T
0.081802 0.750000 0.603508 T T T	0.077746 0.750000 0.602203 T T T
0.572013 0.250000 0.573093 T T T	0.569509 0.250000 0.573108 T T T
0.427987 0.750000 0.426907 T T T	0.430491 0.750000 0.426892 T T T
0.918198 0.250000 0.396492 T T T	0.922254 0.250000 0.397797 T T T
WSe2	MoSe2
1.0	1.0
5.944039 0.000000 0.000000	5.964753 0.000000 0.000000
0.000000 3.301128 0.000000	0.000000 3.281478 0.000000
0.000000 0.000000 20.160000	0.000000 0.000000 20.160000
W Se	Mo Se
2 4	2 4
Selective dynamics	Selective dynamics
Direct	Direct
0.810843 0.750000 0.495938 T T T	0.809643 0.750000 0.496007 T T T
0.189157 0.250000 0.504062 T T T	0.190357 0.250000 0.503993 T T T
0.084550 0.750000 0.593738 T T T	0.082606 0.750000 0.592887 T T T
0.577032 0.250000 0.569474 T T T	0.575259 0.250000 0.569562 T T T
0.422968 0.750000 0.430526 T T T	0.424741 0.750000 0.430438 T T T
0.915450 0.250000 0.406262 T T T	0.917394 0.250000 0.407113 T T T
WS2	MoS2
1.0	1.0
5.711630 0.000000 0.000000	5.722851 0.000000 0.000000
0.000000 3.191390 0.000000	0.000000 3.173255 0.000000
0.000000 0.000000 20.160000	0.000000 0.000000 20.160000
W S	Mo S
2 4	2 4
Selective dynamics	Selective dynamics
Direct	Direct
0.802593 0.750000 0.496539 T T T	0.802497 0.750000 0.496310 T T T
0.197407 0.250000 0.503461 T T T	0.197503 0.250000 0.503690 T T T
0.086405 0.750000 0.586678 T T T	0.083583 0.750000 0.586158 T T T
0.579854 0.250000 0.565748 T T T	0.578635 0.250000 0.565937 T T T
0.420146 0.750000 0.434252 T T T	0.421365 0.750000 0.434063 T T T
0.913595 0.250000 0.413322 T T T	0.916417 0.250000 0.413842 T T T

**Table S2.**

Relaxed atomic structures of 1T'-MX<sub>2</sub> in the VASP/POSCAR format.

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