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Valley-selective circular dichroism of monolayer molybdenum disulphide

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A two-dimensional honeycomb lattice harbours a pair of inequivalent valleys in the *k*-space electronic structure, in the vicinities of the vertices of a hexagonal Brillouin zone, \mathbf{K}_{\pm} . It is particularly appealing to exploit this emergent degree of freedom of charge carriers, in what is termed 'valleytronics'. The physics of valleys mimics that of spin, and will make possible devices, analogous to spintronics, such as valley filter and valve, and optoelectronic Hall devices, all very promising for next-generation electronics. The key challenge lies with achieving valley polarization, of which a convincing demonstration in a two-dimensional honeycomb structure remains evasive. Here we show, using first principles calculations, that monolayer molybdenum disulphide is an ideal material for valleytronics, for which valley polarization is achievable via valley-selective circular dichroism arising from its unique symmetry. We also provide experimental evidence by measuring the circularly polarized photoluminescence on monolayer molybdenum disulphide, which shows up to 50% polarization.

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non-equilibrium charge carrier imbalance between valleys is the key to creating valleytronic devices^{1–9}. The principal mechanism invoked in this context is circularly polarized optical excitation^{3,4}. In this approach, the two valleys absorb left- and right-handed photons differently, a phenomenon referred to as circular dichroism (CD). An essential condition for valley-selective CD in a honeycomb lattice is the absence of a centre of inversion. In the case of graphene, it was suggested that by interacting graphene with a substrate such that the centre of inversion can be obliterated, whereupon a gap opens up in each valley^{10,11}. This strategy, however, is quite challenging experimentally. And even in its eventual realization, there can only be a gentle perturbation to graphene via the weak covalent coupling at large van der Waals separations from the substrate¹¹.

Since its first isolation^{12,13}, monolayer molybdenum disulphide (MoS₂) has attracted immense attention. Many measurements have been performed to characterize the optical and transport properties of this material^{12–16}. In monolayer MoS₂, two layers of sulphur atoms in a two-dimensional hexagonal lattice are stacked over each other in an eclipsed fashion. Each Mo sits in the centre of a trigonal prismatic cage formed by six sulphur atoms (Fig. 1a). Quite remarkably in the context of current discussion, the natural stable structure of free-standing monolayer MoS₂ is a honeycomb lattice with inequivalent bipartite colouring, breaking the inversion symmetry (Fig. 1b).

While bulk MoS₂ has an indirect bandgap, interestingly, when thinned to the monolaver limit, the material acquires direct bandgaps located exactly at the corners of the Brillouin zone. Indeed, with its 1.8 eV direct bandgap and unique two-dimensional structure embracing the high-symmetry valleys, monolayer MoS₂ has much to offer in the exploration of novel electronic and optoelectronic devices and the associated physics (as compared with boron nitride, which has a bandgap of about 6.0 eV in the ultraviolet regime). It is quite natural to question whether it is possible to achieve valleyselective CD in this semiconducting atomic membrane, which will endow electrons in this material the valley degree of freedom, in addition to charge and spin that have been routinely explored in conventional device physics. We show here using ab initio numerical simulation and experimental micro-photoluminescence that monolayer MoS₂ possesses near-perfect valley-selective CD, a property rooted in its bulk symmetry and very much conducive to optoelectronic valley polarization needed for valleytronics.

Results

Degree of circular polarization. The key quantity to assess is, therefore, the k-resolved degree of optical polarization, $\eta(\mathbf{k})$,

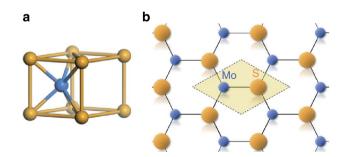


Figure 1 | The crystal structure of monolayer MoS₂. (a) Coordination environment of Mo (blue sphere) in the structure. Sulphur is shown as golden spheres. (b) A top view of the monolayer MoS₂ lattice, emphasizing the connection to a honeycomb lattice. In our calculations, we used an optimized structure at the level of local density approximation in density functional theory. The shaded region bounded by dashed lines corresponds to one primitive cell. The unit cell parameter is a = 3.12 Å, and the vertical separation between sulphur layers is 3.11 Å.

between the top of the valence bands and the bottom of the conduction bands^4

$$\eta(\mathbf{k},\omega_{cv}) = \frac{|\mathcal{P}_{+}^{cv}(\mathbf{k})|^{2} - |\mathcal{P}_{-}^{cv}(\mathbf{k})|^{2}}{|\mathcal{P}_{+}^{cv}(\mathbf{k})|^{2} + |\mathcal{P}_{-}^{cv}(\mathbf{k})|^{2}}.$$
(1)

This quantity is the difference between the absorption of leftand right-handed lights (±), normalized by total absorption, at each **k**-point and evaluated between the top of the valence bands (ν) and the bottom of conduction bands (c). The band structure of monolayer MoS₂ is shown in Fig. 2a. The dependence on the transition energy, $\hbar \omega_{c\nu}(\mathbf{k}) = \varepsilon_c(\mathbf{k}) - \varepsilon_\nu(\mathbf{k})$, is implicit through **k**. Here, the transition matrix element of circular polarization is $\mathcal{P}_{\pm}^{c\nu}(\mathbf{k}) = 1/\sqrt{2}[P_x^{c\nu}(\mathbf{k}) \pm iP_y^{c\nu}(\mathbf{k})]$. The interband matrix elements, $P^{c\nu}(\mathbf{k}) = \langle \psi_{c\mathbf{k}} | \hat{p} | \psi_{\nu\mathbf{k}} \rangle$, are evaluated using the density functional perturbation theory, within the local-density approximation¹⁷, as implemented in VASP¹⁸. Spin-orbit coupling is not included in our calculations^{19,20}. Briefly, a planewave basis set is employed at a

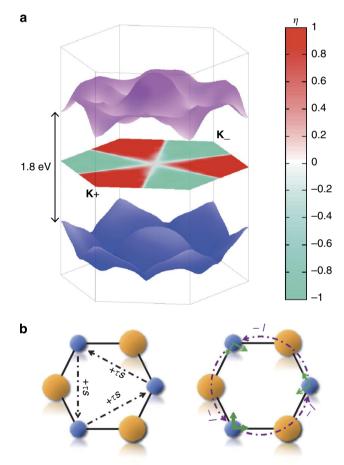


Figure 2 | Valley-selective CD of monolayer MoS₂. (a) Top valence band (blue) and bottom conduction band (pink). The centre hexagon is the Brillouin zone colour-coded by the degree of circular polarization, $\eta(\mathbf{k})$, as defined in the text. The vector connecting \mathbf{K}_+ and \mathbf{K}_- is perpendicular to Mo-S bond in the crystal structure in Fig. 1b. (b) Schematic of phase winding on the MoS₂ lattice that gives rise to the chiral optical selectivity. Left panel: the contribution to phase winding from the Bloch lattice phase, where $\tau = \pm 1$ is the valley index, and s = 1,2 corresponding to the S and Mo sites (isospin index). Right panel: the phase winding under a threefold rotation. The green axes indicate the rotation of local atomic coordinates that leads to the azimuth dissynchronization.

cutoff energy 600 eV, and a total of 80 bands are included to ensure convergence of all computed quantities. A very dense **k**-point mesh (15129 grid points) over the reducible hexagonal Brillouin zone is sampled in our calculations.

As shown in Fig. 2a, chiral absorption selectivity is indeed exact at K_{\pm} with $\eta = \pm 1$. The contrast in the chiral absorptivities between the valleys owes its origin to the symmetry of both lattice and local atomic orbitals, which is quite different from the gapped graphene case⁴. A band state relevant to the optical excitation originates from local atomic states, bearing different orbital magnetic quantum numbers, *l*, or more generally as Wannier function,

$$w_l(\mathbf{r}) = e^{il\varphi} f(\theta, r), \tag{2}$$

where (r,θ,φ) are the standard spherical coordinates taking the *z*-direction perpendicular to the plane of MoS₂. In the case of monolayer MoS₂, the states at the top of the valence bands involve only $d_{x^2-y^2}$ and d_{xy} on Mo, and p_x and p_y states on S. At **K**₊, the *d*-states on Mo hybridize as $1/\sqrt{2}(d_{x^2-y^2}+id_{xy})$ (l=+2) to interact with $1/\sqrt{2}(p_x+ip_y)$ (l=+1). At **K**₋, the *d*-states on Mo hybridize as $1/\sqrt{2}(d_{x^2-y^2}-id_{xy})$ (l=-2) to interact with $1/\sqrt{2}(p_x-ip_y)$ (l=-1). At the bottom of the conduction band, mainly d_{z^2} state on Mo (*l*=0) is involved with a minor contribution from the *p*-orbitals of S. These atomic orbitals form such linear combinations in accordance with the D_{3h} point group symmetry and the lattice translational symmetry.

Microscopic chiral selection rule. The optical selection rule is rooted in the phase winding of the Bloch states under rotational symmetry, threefold rotation (\hat{C}_3) in this case. Given the symmetry-adapted linear combinations of the atomic orbitals, the azimuthal phase associated with the threefold rotation at \mathbf{K}_{\pm} is readily calculable,

$$\hat{C}_3 | v(\mathbf{K}_+) \rangle = | v(\mathbf{K}_+) \rangle, \tag{3}$$

and

$$\hat{C}_{3} \left| c(\mathbf{K}_{\pm}) \right\rangle = e^{\mp i 2\pi/3} \left| c(\mathbf{K}_{\pm}) \right\rangle, \tag{4}$$

where v and c correspond to the valence and conduction band extrema, respectively. Notice, however, the phase winding associated with the rotation has two distinct contributions, as schematically illustrated in Fig. 2b. The first comes from the Bloch phase shift in stepping from one lattice site to a next, as in the case of gapped graphene³. The second phase factor arises as a consequence of dissynchronization of the azimuthal phase (associated with the magnetic quantum number, *l*) concomitant with rotation of local atomic coordinates (green axes in Fig. 2b).

Now the chiral optical selectivity of the valleys can be deduced. The bottom of the conduction bands at the valleys, dominated by the l=0 d-states on Mo, bears an overall azimuthal quantum number $m_{\pm} = \pm 1$, at \mathbf{K}_{\pm} . At the top of the valence bands, $m_{\pm} = 0$. Then for an optical transition at \mathbf{K}_{\pm} , the angular momentum selection rule indicates that $\Delta m_{\pm} = \pm 1$, corresponding to the absorption of left- and right-handed photons. Therefore, our density functional perturbation theory results concerning the close neighbourhood of the valleys, which is most important to the proposed optical valley polarization, are in fact ensured by the symmetry of the material.

There is an important distinction, compared with gapped graphene, in the microscopic origin of chiral optical selection rule; that is, the selectivity arises directly from the local relative azimuthal phase of the atomic orbitals, in contrast to the sublattice-dependent Bloch phase winding in the case of gapped graphene³. The bonding of the electronic states in MoS_2 across the gap is also considerably more complex, exhibiting richer possibilities of variation owing to the symmetry of local atomic states. Remarkably, the selectivity is nearly perfect over the entire valleys, and only changes sign rapidly across valley boundaries (Fig. 2a). This is to say, the entire valley K_+ absorbs almost purely left-handed photons, whereas the entire valley K_- purely right-handed. The perfect intrinsic valley-constrasting CD is very much conducive to optical polarization of the valleys. When a left (right)-handed light is shone over the sample, a non-equilibrium state will be created where the charge carrier population resides mostly in K_+ (K_-) valley (valley polarization).

Circularly polarized photoluminescence. To further confirm our theoretical and numerical results, we have also performed experimental circularly polarized photoluminescence (PL) measurements on monolayer MoS₂. The polarization of PL is an indication of how good the chiral optical selectivity is, and of how well the valley identity of charge carriers is preserved before recombination. Fig. 3a,b

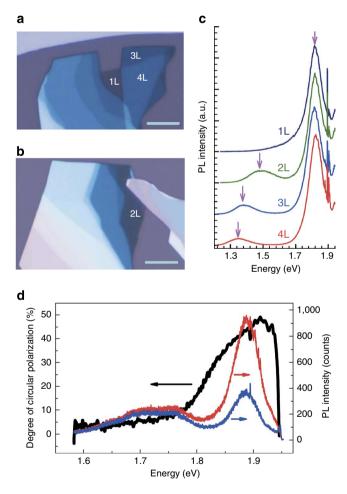


Figure 3 | Experimental measurements of circularly polarized PL of monolayer MoS₂. (a) and (b) Optical images of one-to-four-layer samples (1L to 4L) on which micro-PL is performed, where 1L, 2L, 3L and 4L regions are labelled. The scale bars correspond to 5 microns. (c) Micro-PL of monolayer and few-layer MoS₂ at 300 K. Each spectrum is normalized by its maximum intensity. Arrows indicate the lowest-energy peak of each spectrum. (d) Circularly polarized micro-PL of monolayer MoS₂ at 83 K, along with the degree of circular polarization of the PL spectra. The red and blue curves correspond to the intensities of σ^+ and σ^- polarizations, respectively, in the luminescence spectrum. The black curve is the net degree of polarization.

show the samples on which our experiments are performed. The monolayer region is identified by micro-PL at 300 K (Fig. 3c), as in a monolayer sample displays a single PL peak at 1.82 eV, while multi-layer samples show an additional peak at lower energies¹². In Fig. 3d, we show the intensities of the luminescence with σ^+ (left-handed) and σ^- (right-handed) polarizations at low temperature (83 K), under a σ^+ irradiation at wavelength 633 nm (see Methods). In agreement with our prediction, the luminescence indeed exhibits a substantial circular polarization (η ~50%) at the PL peak.

Discussion

The experimentally measured polarization of the PL is considerably larger than spin-related polarization in other widely studied materials such as GaAs, but smaller than the expected value from *ab initio* simulation ($\eta \ge 0.98$ for the energy of the incident light). There are two important timescales in the valley-optical processes: valley lifetime, τ_v , and recombination time, $\tau^{-1} = \tau_r^{-1} + \tau_{nr}^{-1}$, in which subscripts r and nr refer to radiative and non-radiative recombinations (via, for example, the substrate), respectively. The value of polarization of the experimental PL, η_{PL} , can be deduced from standard rate equations for the steady-state process,

$$\frac{\eta_{\rm PL}}{\eta} = \frac{(1-\delta)^2}{1+\tau/\tau_{\nu}},\tag{5}$$

where $1-\delta$ is selectivity in the initial excitation (including possible intervalley generation), and η the theoretical degree of circular polarization.

In the lowest order description of the kinetic processes, we have $\delta = \delta_{imp} + \delta_{ph}$ to account for impurity/defects/substrate- and phonon-assisted excitation and recombination in which the valleys are coupled by the momentum components of the scatterers. Consequently, the less-than-perfect circular polarization observed in the experimental PL is ascribable to inevitable intervalley processes, or relatively large ratio between valley lifetime and recombination time, τ/τ_{ν} . Measurements of PL circular polarization on high-quality, clean samples at very low temperatures (minimizing δ) will allow the extraction of τ/τ_{ν} . Moreover, it is interesting to assess the role of non-radiative relaxation of carriers, which can be induced by substrate¹² and defects.

Now that we have established the valley-selective CD in monolayer MoS₂ with ensuing non-equilibrium valley polarization, it is also interesting to inspect the Berry curvature, $\Omega_n(\mathbf{k}) = \Omega_{n,z}(\mathbf{k})\hat{z}$, which, if present, has crucial influence on the electronic transport properties. Berry curvature enters into the semiclassical wavepacket dynamics via an anomalous velocity perpendicular to the applied electric field (~ $\mathbf{E} \times \Omega_n(\mathbf{k})$), in addition to the usual group velocity of a Bloch band state^{21,22}. Although Berry curvature is not exactly a ground-state property, it can be evaluated quite accurately for the Kohn-Sham one-particle states^{23,24}. The presence of non-vanishing Berry curvature is possible in the non-centrosymmetric honeycomb lattice³. In Fig. 4, we plot the Berry curvature, $\Omega_{n,z}(\mathbf{k}) = -2 \operatorname{Im} \langle \partial u_{n\mathbf{k}} / \partial k_x | \partial u_{n\mathbf{k}} / \partial k_y \rangle$ along the $\mathbf{K}_- - \Gamma - \mathbf{K}_+$ path. Because the system has time-reversal symmetry and not inversion symmetry, $\Omega_{n,z}(\mathbf{k})$ is an odd function in \mathbf{k} with generally non-zero values, as expected. The charge carriers' anomalous velocities acquire opposite signs in the two valleys, exactly cancelling each other's contribution to the transverse current. At equilibrium, freestanding monolayer MoS₂ will not exhibit valley Hall effect, as expected. At \mathbf{K}_{\pm} , the Berry curvatures do not have the particle-hole symmetry. This is a clear indication that the physics of MoS₂ cannot be fully captured by a minimalistic two-band model, as is distinct from the case of gapped graphene.

On the bais of our theoretical and experimental results, a few further experiments are quite compelling. When valley polarization

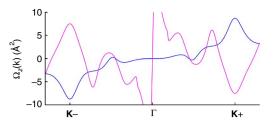


Figure 4 | Berry curvature, $\Omega_{n,z}(\mathbf{k})$, of bands across the bandgap. The blue curve corresponds to the top of valence bands. The red curve corresponds to the bottom of conduction bands. The Berry curvatures of the states along the $\mathbf{K}_{-} - \Gamma - \mathbf{K}_{+}$ path of the Brillouin zone are plotted. The value of Berry curvature is large for the conduction band at the zone centre, where bands are degenerate.

is induced by, say, valley-selective CD, only one valley has nonvanishing charge carrier population (ideally, assuming the absence of intervalley scattering). This can then lead to the Hall effect and magnetization without an applied magnetic field⁴. The Berry curvature across the band edges near K_{\pm} is most relevant to photo-excited charge carriers. We see that, at the band edges, both conduction and valence bands display significant Berry curvature with opposite signs. Consequently, when electrons and holes are generated by a circularly polarized irradiation, both types of charge carriers have an intrinsic concurrent contribution to the Hall conductivity or magnetization.

Moreover, a time-resolved PL measurement will also be an interesting experiment for revealing the valley lifetime, analogous to the spin lifetime in spintronics. In closing, we also would like to point out that MoS₂ is but one of the many transition metal dichalcogenides, MX₂, where M = Mo, W, and X = S, Se. They all have identical crystal structure and are similar electronically. These compounds, once available in monolayer form, will provide a chemically rich family of semiconducting atomic membranes for exploring the valley physics, as we have demonstrated here for MoS₂. In addition, there is considerable spin-orbit coupling in these systems¹⁹, and the valley and spin dependent physics in the neighbourhood of K points in MoX₂ monolayers is discussed in a recent theoretical work²⁰. The evaluation of optical selecivity and Berry curvature at higher level theories to address the many-body nature of the excited states is also an important future direction.

Methods

Sample preparation. MoS_2 flakes consisting of 1–4 layers (L) are obtained by micro-mechanical cleavage of a natural bulk MoS_2 crystal (SPI Supplies, USA) on a Si/90 nm SiO₂ substrate. The number of layers is identified by optical contrast and PL spectroscopy.

Circularly polarized micro-PL. Optical contrast and micro-PL are performed in a backscattering geometry using a Jobin-Yvon HR800 Raman system equipped with a liquid-nitrogen-cooled charge-coupled detector. The optical excitation wavelength is 633 nm from a HeNe laser. The laser beam passes through a Soleil Babinet Compensator to generate a circularly polarized light. The polarization is set to σ^+ , and the PL polarization σ^+ or σ^- is analysed by a quarter-wave plate placed in front of a fixed Glan-Thomson linear polarizer. The whole set-up provides a rejection ratio better than 5% in σ^+ and σ^- configuration over the spectral range of interest. The excitation power of 50 μ W is used to avoid sample heating. We use a normal x100 objective with numerical aperture =0.90 for optical contrast and PL measurement at room temperature (Fig. 3c). A long-working-distance ×50 objective is used for PL measurement at low temperature (Fig. 3d). The sample temperature was controlled by a programmable hot stage THMS600 from Linkam Scientific Instruments.

References

- . Rycerz, A., Tworzydlo, J. & Beenakker, C. W. J. Valley filter and valley valve in graphene. *Nat. Phys.* **3**, 172–175 (2007).
- Akhmerov, A. R. & Beenakker, C. W. J. Detection of valley polarization in graphene by a superconducting contact. *Phys. Rev. Lett.* 98, 157003 (2007).

- Yao, W., Xiao, D. & Niu, Q. Valley-dependent optoelectronics from inversion symmetry breaking. *Phys. Rev. B* 77, 235406 (2008).
- Gunawan, O. *et al.* Valley susceptibility of an interacting two-dimensional electron system. *Phys. Rev. Lett.* 97, 186404 (2006).
- Takashina, K., Ono, Y., Fujiwara, A., Takahashi, Y. & Hirayama, Y. Valley polarization in Si(100) at zero magnetic field. *Phys. Rev. Lett.* 96, 236801 (2006).
- Bishop, N. C. et al. Valley polarization and susceptibility of composite Fermions around a filling factor v=2/3. Phys. Rev. Lett. 98, 266404 (2007).
- Eng, K., McFarland, R. N. & Kane, B. E. Integer quantum Hall effect on a sixvalley hydrogen-passivated silicon (111) surface. *Phys. Rev. Lett.* 99, 016801 (2007).
- Zhu, Z., Collaudin, A., Fauque, B., Kang, W. & Behnia, K. Field-induced polarization of Dirac valleys in bismuth. *Nat. Phys.* 8, 89–94 (2011).
- Giovannetti, G., Khomyakov, P. A., Brocks, G., Kelly, P. J. & van den Brink, J. Substrate-induced band gap in graphene on hexagonal boron nitride: *Ab initio* density functional calculations. *Phys. Rev. B* 76, 073103 (2007).
- Zhou, S. Y. *et al.* Substrate-induced bandgap opening in epitaxial graphene. *Nat. Mater.* 6, 770–775 (2007).
- Mak, K. F., Lee, C., Hone, J., Shan, J. & Heinz, T. F. Atomically thin MoS₂: a new direct-gap semiconductor. *Phys. Rev. Lett.* **105**, 136805 (2010).
- Lee, C. et al. Anomalous lattice vibrations of single- and few-layer MoS₂. ACS Nano 4, 2695–2700 (2010).
- Splendiani, A. *et al.* Emerging photoluminescence in monolayer MoS₂. *Nano Lett.* 10, 1271–1275 (2010).
- Ramakrishna Matte, H. S. S. *et al.* MoS₂ and WS₂ analogues of graphene. Angew. Chem. **122**, 4153–4156 (2010).
- Radisavljevic, B., Radenovic, A., Brivio, J., Giacometti, V. & Kis, A. Single-layer MoS₂ transistors. *Nat. Nanotech.* 6, 147–150 (2011).
- Ceperley, D. M. & Alder, B. J. Ground state of the electron gas by a stochastic method. *Phys. Rev. Lett.* 45, 566–569 (1980).
- Gajdoš, M., Hummer, K., Kresse, G., Furthmüller, J. & Bechstedt, F. Linear optical properties in the projector-augmented wave methodology. *Phys. Rev. B* 73, 045112 (2006).
- Zhu, Z. Y., Cheng, Y. C. & Schwingenschlögl, U. Giant spin-orbit-induced spin splitting in two-dimensional transition-metal dichalcogenide semiconductors. *Phys. Rev. B* 84, 153402 (2011).

- Xiao, D., Liu, G.- B., Feng, W., Xu, X. & Yao, W. Coupled spin and valley physics in monolayers of MoS₂ and other group-VI dichalcogenides. *Phys. Rev. Lett.* 108, 196802 (2012).
- 21. Karplus, R. & Luttinger, J. M. Hall effect in ferromagnetics. *Phys. Rev.* 95, 1154–1160 (1954).
- Chang, M.- C. & Niu, Q. Berry phase, hyperorbits, and the hofstadter spectrum. *Phys. Rev. Lett.* **75**, 1348–1351 (1995).
- Yao, Y. et al. First principles calculation of anomalous Hall conductivity in ferromagnetic bcc Fe. Phys. Rev. Lett. 92, 037204 (2004).
- Malashevich, A. & Vanderbilt, D. First principles study of improper ferroelectricity in TbMnO₂. *Phys. Rev. Lett.* **101**, 037210 (2008).

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Author contribution

J.F. and Q.N. conceived the research. T.C., J.F. and E.W. performed coding and calculations. W.H. prepared the samples. G.W., W.H., H.Y., C.Z., P.T. and B.L. performed PL measurements. B.L. conceived and coordinated the experimental investigations. J.F., J.S. and T.C. performed theoretical analysis. J.F., J.S., B.L., T.C. and P.T. wrote the manuscript, which all authors read and commented on. J.F. and E.W. are responsible for coordinating the project.

Additional information

Competing financial interests: The authors declare no competing financial interests.

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